



Figure 11.1. Advance-purchase and max-stay restrictions for an airline trip represented by a grid in a two-dimensional space. Customer's ideal point is the most restrictive point in this space where they have the highest valuation.

customer's  $i$ 's valuation for product  $j$ . This however would create estimation difficulties, so below we use a simpler additive model in the spirit of the conjoint utility model of Section 11.1.

Let customer  $i$  have an *ideal point* defined as follows: it is the most restrictive product  $j$  for which he has his maximum valuation. For example, in Figure 11.1, customer  $i$ 's uncertainty about his trip is resolved somewhere between 7 and 14 days before his trip date, and his trip takes more than 6 days and less than 1 month. Then his ideal point is represented by the potential product with restrictions of max-stay of 1 month and advance-purchase restriction of 7 days. Let his valuation for the product at this ideal point be  $v$ . If however, for reasons of price or availability, he is forced to purchase 14 days in advance, his willingness to pay would be lower. We model this as a reduction in valuation for purchasing less-than-ideal products.

Let  $w_{jk}$  represent the disutility for a customer whose ideal point is product  $j$ , if he has to purchase product  $k$ . (It is conceivable that this reduction is zero, especially when a customer purchases a less restrictive product.) If consumer  $i$ 's ideal product is  $j_i$ , then his net utility for purchasing product  $k$  is given by  $v - w_{j_i k} - p_k$ , where  $p_k$  is the price charged by the firm for product  $k$ . So far we have assumed all the valuations  $v$  and  $w$ 's are deterministic, but they could also be modeled as random variables to be more realistic. To keep the exposition simple, we assume